

Exercises – 15 A

- Q. 1 **Answer :**
- Sum of the angles of a triangle is 180° .
- $$\therefore \angle A + \angle B + \angle C = 180^\circ$$
- $$72^\circ + 63^\circ + \angle C = 180^\circ$$
- $$\angle C = 45^\circ$$
- Hence, $\angle C$ measures 45° .
- Q. 2 **Answer :**
- Sum of the angles of any triangle is 180° .
- In $\triangle DEF$:
- $$\angle D + \angle E + \angle F = 180^\circ$$
- $$\angle D + 105^\circ + 40^\circ = 180^\circ$$
- $$\text{or } \angle D = 180^\circ - (105^\circ + 40^\circ)$$
- $$\text{or } \angle D = 35^\circ$$
- Q. 3 **Answer :**
- Sum of the angles of any triangle is 180° .
- In $\triangle DEF$:
- $$\angle D + \angle E + \angle F = 180^\circ$$
- $$\angle D + 105^\circ + 40^\circ = 180^\circ$$
- $$\text{or } \angle D = 180^\circ - (105^\circ + 40^\circ)$$
- $$\text{or } \angle D = 35^\circ$$
- Q. 4 **Answer :**
- Suppose the angles of the triangle are $(4x)^\circ$, $(3x)^\circ$ and $(2x)^\circ$.
- Sum of the angles of any triangle is 180° .
- $$\therefore 4x + 3x + 2x = 180$$
- $$9x = 180$$
- $$x = 20$$
- Therefore, the angles of the triangle are $(4 \times 20)^\circ$, $(3 \times 20)^\circ$ and $(2 \times 20)^\circ$, i.e. 80° , 60° and 40° .
- Q. 5 **Answer :**
- Sum of the angles of a triangle is 180° .
- Suppose the other angle measures x .
- It is a right angle triangle. Hence, one of the angle is 90° .
- $$\therefore 36^\circ + 90^\circ + x = 180^\circ$$
- $$x = 54^\circ$$
- Hence, the other angle measures 54° .

Q. 6

Answer :

Suppose the acute angles are $(2x)^\circ$ and $(x)^\circ$

Sum of the angles of any triangle is 180°

$$\therefore 2x + x + 90 = 180$$

$$\Rightarrow (3x) = 180 - 90$$

$$\Rightarrow (3x) = 90$$

$$\Rightarrow x = 30$$

So, the angles measure $(2 \times 30)^\circ$ and 30° i.e. 60° and 30°

Q. 7

Answer :

The other two angles are equal. Let one of these angles be x° .

Sum of angles of any triangle is 180° .

$$\therefore x + x + 100 = 180$$

$$2x = 80$$

$$x = 40$$

Hence, the equal angles of the triangle are 40° each.

Q. 8

Answer :

Suppose the third angle of the isosceles triangle is x° .

Then, the two equal angles are $(2x)^\circ$ and $(2x)^\circ$.

Sum of the angles of any triangle is 180° .

$$\therefore 2x + 2x + x = 180$$

$$5x = 180$$

$$x = 36$$

Hence, the angles of the triangle are 36° , $(2 \times 36)^\circ$ and $(2 \times 36)^\circ$, i.e. 36° , 72° and 72° .

Q. 9

Answer :

Suppose the angles are $\angle A$, $\angle B$ and $\angle C$.

(Sum of the angles of a triangle is 180°)

Given :

$$\angle A = \angle B + \angle C$$

$$\text{Also, } \angle A + \angle B + \angle C = 180^\circ$$

$$\therefore \angle A + \angle A = 180^\circ$$

$$\Rightarrow 2\angle A = 180^\circ$$

$$\Rightarrow \angle A = 90^\circ$$

Hence, the triangle ABC is right angled at $\angle A$.

Q. 10

Answer :

Suppose: $2\angle A = 3\angle B = 6\angle C = x^\circ$

Then, $\angle A = \left(\frac{x}{2}\right)^\circ$

$\angle B = \left(\frac{x}{3}\right)^\circ$ and $\angle C = \left(\frac{x}{6}\right)^\circ$

Sum of the angles of any triangle is 180° .

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\Rightarrow \frac{x}{2} + \frac{x}{3} + \frac{x}{6} = 180^\circ$$

$$\Rightarrow \frac{3x + 2x + x}{6} = 180^\circ$$

$$\Rightarrow \frac{6x}{6} = 180^\circ$$

$$\Rightarrow x = 180$$

$$\therefore \angle A = \left(\frac{180}{2}\right)^\circ = 90^\circ$$

$$\angle B = \left(\frac{180}{3}\right)^\circ = 60^\circ$$

$$\angle C = \left(\frac{180}{6}\right)^\circ = 30^\circ$$

Q. 11

Answer :

We know that the angles of an equilateral triangle are equal.

Let the measure of each angle of an equilateral triangle be x° .

$$\therefore x + x + x = 180$$

$$x = 60$$

Hence, the measure of each angle of an equilateral triangle is 60° .

Q. 12

Answer :

(i)

$DE \parallel BC$

$$\therefore \angle ABC = \angle ADE = 55^\circ$$

(Corresponding angles)

(ii) Sum of the angles of any triangle is 180° .

$$\therefore \angle A + \angle B + \angle C = 180^\circ$$

$$\angle C = 180^\circ - (65^\circ + 55^\circ) = 60^\circ$$

$DE \parallel BC$

$$\therefore \angle AED = \angle ACB = 60^\circ \quad (\text{corresponding angles})$$

(iii) We have found in point (ii) that $\angle C$ is equal to 60° .

Exercises – 15 B

Q. 1

Answer :

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\angle ACD = \angle CAB + \angle CBA$$

$$\angle ACD = 75^\circ + 45^\circ = 120^\circ$$

Q. 2

Answer :

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\therefore \angle BAC + \angle ABC = \angle ACD$$

$$x + 68 = 130$$

$$x = 62$$

Sum of the angles in any triangle is 180° .

$$\therefore \angle BAC + \angle ABC + \angle ACB = 180^\circ$$

$$62 + 68 + y = 180$$

$$y = 50$$

Q. 3

Answer :

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\therefore \angle BAC + \angle CBA = \angle ACD$$

$$32 + x = 65$$

$$x = 33$$

Also, sum of the angles in any triangle is 180° .

$$\therefore \angle BAC + \angle CBA + \angle ACB = 180^\circ$$

$$32 + 33 + y = 180$$

$$y = 115$$

$$\therefore x = 33$$

$$y = 115$$

Q. 4

Answer :

Suppose the interior opposite angles are $(2x)^\circ$ and $(3x)^\circ$.

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\therefore 3x + 2x = 110$$

$$x = 22$$

The interior opposite angles are $(2 \times 22)^\circ$ and $(3 \times 22)^\circ$, i.e. 44° and 66° .

Suppose the third angle of the triangle is y° .

Now, sum of the angles in any triangle is 180° .

$$\therefore 44 + 66 + y = 180$$

$$y = 70$$

Hence, the angles of the triangle are 44° , 66° and 70° .

Q. 5

Answer :

Suppose the interior opposite angles of an exterior angle 100° are x° and x° .

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\therefore x + x = 100$$

$$2x = 100$$

$$x = 50$$

Also, sum of the angles of any triangle is 180° .

Let the measure of the third angle be y° .

$$\therefore x + x + y = 180$$

$$50 + 50 + y = 180$$

$$y = 80$$

Hence, the angles are of the measures 50° , 50° and 80° .

Q. 6

Answer :

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

In $\triangle ABC$:

$$\angle ACD = \angle BAC + \angle ABC = 25^\circ + 45^\circ$$

$$\angle ACD = 70^\circ$$

(ii) In $\triangle ECD$:

$$\angle AED = \angle ECD + \angle EDC = 70^\circ + 40^\circ$$

$$\Rightarrow \angle AED = 110^\circ$$

Q. 7

Answer :

Sum of the angles of a triangle is 180° .

In $\triangle ABC$:

$$\angle BAC + \angle CBA + \angle ACB = 180^\circ$$

$$\angle BAC = 180^\circ - (40^\circ + 100^\circ)$$

$$\Rightarrow \angle BAC = 40^\circ$$

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\angle ACD = \angle BAC + \angle CBA = 40^\circ + 40^\circ = 80^\circ$$

$$(i) \angle ACD = 80^\circ$$

(ii) In $\triangle ACD$:

$$\angle CAD + \angle ACD + \angle ADC = 180^\circ$$

$$\Rightarrow \angle ADC = 180^\circ - (50^\circ + 80^\circ)$$

$$\Rightarrow \angle ADC = 50^\circ$$

$$\therefore \angle ADC = 50^\circ$$

$$(iii) \angle DAB + \angle DAE = 180^\circ \quad (\text{since } BE \text{ is a straight line})$$

$$\angle DAE = 180^\circ - (\angle DAC + \angle CAB)$$

$$\angle DAE = 180^\circ - (50^\circ + 40^\circ)$$

$$\angle DAE = 90^\circ$$

Q. 8

Answer :

$$\begin{aligned}\frac{x}{y} &= \frac{2}{3} \\ \Rightarrow 3x &= 2y \\ \Rightarrow x &= \frac{2}{3}y\end{aligned}$$

We know that the exterior angle of a triangle is equal to the sum of the interior opposite angles.

$$\therefore \angle A + \angle B = \angle ACD$$

$$x^\circ + y^\circ = 130^\circ$$

$$\begin{aligned}\Rightarrow \frac{2y}{3} + y &= 130 \\ \Rightarrow 5y &= 130 \times 3 \\ \Rightarrow 5y &= 390 \\ \Rightarrow y &= 78 \\ \Rightarrow x &= \frac{2}{3} \times 78 \\ \Rightarrow x &= 52\end{aligned}$$

Also, sum of the angles in any triangle is 180°

$$\begin{aligned}\therefore x + y + z &= 180 \\ z &= 180 - 78 - 52 \\ z &= 50\end{aligned}$$

Exercises – 15 C

Q. 1

Answer :

(i) Consider numbers 1, 1 and 1.

Clearly, $1 + 1 > 1$

$$1 + 1 > 1$$

$$1 + 1 > 1$$

Thus, the sum of any two sides is greater than the third side.

Hence, it is possible to draw a triangle having sides 1 cm, 1 cm and 1 cm.

(ii)

Clearly, $2 + 3 > 4$

$$3 + 4 > 2$$

$$2 + 4 > 3$$

Thus, the sum of any two sides is greater than the third side.

Hence, it is possible to draw a triangle having sides 2 cm, 3 cm and 4 cm.

(iii)

Clearly, $7 + 8 = 15$

Thus, the sum of these two numbers is not greater than the third number.

Hence, it is not possible to draw a triangle having sides 7 cm, 8 cm and 15 cm.

(iv) Consider the numbers 3.4, 2.1 and 5.3.

Clearly: $3.4 + 2.1 > 5.3$

$$5.3 + 2.1 > 3.4$$

$$5.3 + 3.4 > 2.1$$

Thus, the sum of any two sides is greater than the third side.

Hence, it is possible to draw a triangle having sides 3.4 cm, 2.1 cm and 5.3 cm.

(v) Consider the numbers 6, 7 and 14.

Clearly, $6 + 7 < 14$

Thus, the sum of these two numbers is not greater than the third number.

Hence, it is not possible to draw a triangle having sides 6 cm, 7 cm and 14 cm.

Q. 2

Answer :

Let the length of the third side be x cm.

Sum of any two sides of a triangle is greater than the third side.

$$\therefore 5 + 9 > x$$

$$\Rightarrow x < 14$$

Hence, the length of the third side must be less than 14 cm.

Q. 3

Answer :

(i) $>$

(ii) $>$

(iii) $<$

The reason for the above three is that the sum of any two sides of a triangle is greater than the third side.

Q. 4

Answer :

Sum of any two sides of a triangle is greater than the third side.

In $\triangle AMB$:

$$AB + BM > AM \dots\dots (i)$$

In $\triangle AMC$:

$$AC + CM > AM \dots\dots (ii)$$

Adding the above two equation:

$$AB + BM + AC + CM > AM + AM$$

$$AB + BC + AC > 2AM$$

Hence, proved.

Q. 5

Answer :

Sum of any two sides of a triangle is greater than the third side.

In $\triangle APB$:

$$AB + BP > AP$$

In $\triangle APC$:

$$AC + PC > AP$$

Adding the correspondong sides :

$$AB + BP + AC + PC > AP + AP$$

$$AB + AC + BC > 2AP$$

Hence, proved.

Q. 6

Answer :

Sum of any two sides of a triangle is greater than the third side.

In $\triangle ABC$:

$$AB + BC > AC$$

In $\triangle ADC$:

$$CD + DA > AC$$

Adding the above two:

$$AB + BC + CD + DA > 2 AC \quad \dots (i)$$

In $\triangle ADB$:

$$AD + AB > BD$$

In $\triangle BDC$:

$$CD + BC > BD$$

Adding the above two:

$$AB + BC + CD + DA > 2 BD \quad \dots (ii)$$

Adding equation (i) and (ii):

$$AB + BC + CD + DA + AB + BC + CD + DA > 2(AC + BD)$$

$$\Rightarrow 2(AB + BC + CD + DA) > 2(AC + BD)$$

$$\Rightarrow AB + BC + CD + DA > AC + BD$$

Q. 7

Answer :

We know that the sum of any two sides of a triangle is greater than the third side.

In $\triangle AOB$:

$$OA + OB > AB \dots (1)$$

In $\triangle BOC$:

$$OB + OC > BC \dots (2)$$

In $\triangle AOC$:

$$OA + OC > CA \dots (3)$$

Adding (1), (2) and (3):

$$OA + OB + OB + OC + OA + OC > AB + BC + CA$$

$$2(OA + OB + OC) > AB + BC + CA$$

Hence, proved.

Exercises – 15 D

Q. 1

Answer :

Suppose the length of the hypotenuse is a cm.

Then, by Pythagoras theorem:

$$\begin{aligned}a^2 &= 9^2 + 12^2 \\ \Rightarrow a^2 &= 81 + 144 \\ \Rightarrow a^2 &= 225 \\ \Rightarrow a &= \sqrt{225} \\ \Rightarrow a &= 15\end{aligned}$$

Hence, the length of the hypotenuse is 15 cm.

Q. 2

Answer :

Suppose the length of the other side is a cm.

Then, by Pythagoras theorem:

$$\begin{aligned}26^2 &= 10^2 + a^2 \\ \Rightarrow a^2 &= 676 - 100 \\ \Rightarrow a^2 &= 576 \\ \Rightarrow a &= \sqrt{576} \\ \Rightarrow a &= 24\end{aligned}$$

Hence, the length of the other side is 24 cm.

Q. 3

Answer :

Suppose the length of the other side is a cm.

Then, by Pythagoras theorem:

$$\begin{aligned}4.5^2 + a^2 &= 7.5^2 \\ \Rightarrow a^2 &= 56.25 - 20.25 \\ \Rightarrow a^2 &= 36 \\ \Rightarrow a &= \sqrt{36} \\ \Rightarrow a &= 6\end{aligned}$$

Hence, the length of the other side of the triangle is 6 cm.

Q. 4

Answer :

Suppose the length of the two legs of the right triangle are a cm and a cm.

Then, by Pythagoras theorem:

$$\begin{aligned}a^2 + a^2 &= 50 \\ \Rightarrow 2a^2 &= 50 \\ \Rightarrow a^2 &= 25 \\ \Rightarrow a &= \sqrt{25} \\ \Rightarrow a &= 5\end{aligned}$$

Hence, the length of each leg is 5 cm.

Q. 5

Answer :

The largest side of the triangle is 39 cm.

$$15^2 + 36^2 \\ = 225 + 1296 = 1521$$

$$\text{Also, } 39^2 = 1521 \\ \therefore 15^2 + 36^2 = 39^2$$

Sum of the square of the two sides is equal to the square of the third side.

Hence, the triangle is right angled.

Q. 6

Answer :

Suppose the length of the hypotenuse is c cm.

Then, by Pythagoras theorem:

$$a^2 + b^2 = c^2 \\ \Rightarrow c^2 = 6^2 + 4.5^2 \\ \Rightarrow c^2 = 36 + 20.25 \\ \Rightarrow c^2 = 56.25 \\ \Rightarrow c = \sqrt{56.25} \\ \Rightarrow c = 7.5$$

Hence, the length of its hypotenuse is 7.5 cm.

Q. 7

Answer :

(i) Largest side, $c = 25$ cm

We have:

$$a^2 + b^2 = 225 + 400 = 625$$

$$\text{Also, } c^2 = 625$$

$$\therefore a^2 + b^2 = c^2$$

Hence, the given triangle is right angled using the Pythagoras theorem.

(ii) Largest side, $c = 16$ cm

We have:

$$a^2 + b^2 = 81 + 144 = 225$$

$$\text{Also, } c^2 = 256$$

$$\text{Here, } a^2 + b^2 \neq c^2$$

Therefore, the given triangle is not right angled.

Q. 8

Answer :

We have:

$$\angle B = 35^\circ \text{ and } \angle C = 55^\circ$$

$$\therefore \angle B = 180 - 35 - 55 = 90^\circ \quad (\text{since sum of the angles of any triangle is } 180^\circ)$$

We know that the side opposite to the right angle is the hypotenuse.

By Pythagoras theorem:

$$BC^2 = AB^2 + AC^2$$

Hence, (iii) is true.

Q. 9

Answer :

By Pythagoras theorem in $\triangle ABC$:

$$AB^2 = AC^2 + BC^2$$

$$152 = x^2 + 122 \Rightarrow x^2 = 225 - 144 \Rightarrow x^2 = 81 \Rightarrow x = 9$$

$$\therefore x = 9 \text{ cm}$$

Hence, the distance of the foot of the ladder from the wall is 9 cm.

Q. 10

Answer :

Suppose the foot of the ladder is x m far from the wall.

Let the ladder is represented by AB , the height at which it reaches the wall be AC and the distance between the foot of ladder and wall be BC .

Then, by Pythagoras theorem:

$$AB^2 = AC^2 + BC^2$$

$$\Rightarrow 5^2 = 4.8^2 + x^2$$

$$\Rightarrow x^2 = 25 - 23.04$$

$$\Rightarrow x^2 = 1.96$$

$$\Rightarrow x^2 = (1.4)^2$$

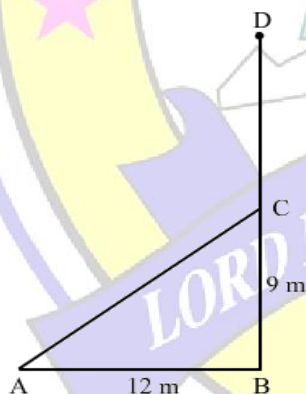
$$\Rightarrow x = 1.4$$

Hence, the foot of the ladder is 1.4 m far from the wall.

Q. 11

Answer :

Let BD be the height of the tree broken at point C and suppose CD take the position CA



Now as per given conditions we have $AB = 9 \text{ m}$, $BC = 12 \text{ m}$

By Pythagoras theorem:

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow AC^2 = 12^2 + 9^2$$

$$\Rightarrow AC^2 = 144 + 81$$

$$\Rightarrow AC^2 = 225$$

$$\Rightarrow AC^2 = 15^2$$

$$\Rightarrow AC = 15$$

Length of the tree before it broke = $AC + AB$

$$= 15 + 9$$

$$= 24 \text{ m}$$

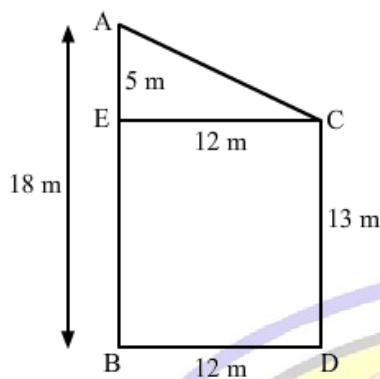
Q. 12

Answer :

Suppose, the two poles are AB and CD, having the length of 18 m and 13 m, respectively.

Distance between them, BD, is equal to 12 m.

We need to find AC.



From C, draw $CE \perp AB$.

$$AE = AB - EB$$

$$= AB - CD \quad (CD = EB)$$

$$= 18 - 13$$

$$= 5 \text{ m}$$

$$EC = BD = 12 \text{ m}$$

Now, by Pythagoras theorem in $\triangle AEC$:

$$AC^2 = AE^2 + EC^2$$

$$\Rightarrow AC^2 = 5^2 + 12^2$$

$$\Rightarrow AC^2 = 25 + 144$$

$$\Rightarrow AC^2 = 169$$

$$\Rightarrow AC^2 = 13^2$$

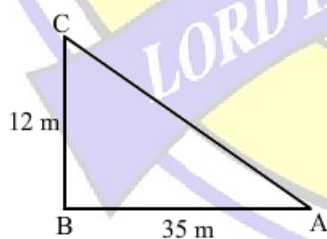
$$\Rightarrow AC = 13$$

Hence, the distance between their tops is 13 m.

Q. 13

Answer :

Suppose the man starts at point A and goes 35 m towards west, say AB. He then goes 12 m north, say BC.



We need to find AC.

By Pythagoras theorem:

$$AC^2 = BC^2 + AB^2$$

$$\Rightarrow AC^2 = 35^2 + 12^2$$

$$\Rightarrow AC^2 = 1225 + 144$$

$$\Rightarrow AC^2 = 1369$$

$$\Rightarrow AC^2 = 37^2$$

$$\Rightarrow AC = 37 \text{ m}$$

Hence, the man is 37 m far from the starting point.

Q. 14

Answer :

Suppose the man starts from A and goes 3 km north and reaches B.
He then goes 4 km towards east and reaches C.

$$\therefore AB = 3 \text{ km}$$

$$BC = 4 \text{ km}$$

We have to find AC.

By Pythagoras theorem:

$$\Rightarrow AC^2 = AB^2 + BC^2$$

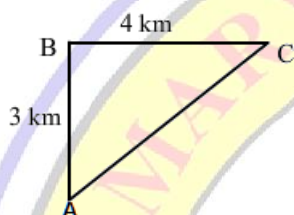
$$\Rightarrow AC^2 = 3^2 + 4^2$$

$$\Rightarrow AC^2 = 25$$

$$\Rightarrow AC^2 = 5^2$$

$$\Rightarrow AC = 5 \text{ km}$$

Hence, he is 5 km far from the initial position.



Q. 15

Answer :

Suppose the sides are x and y of lengths 16 cm and 12 cm, respectively.

Let the diagonal be z cm.

Clearly, the diagonal is the hypotenuse of the right triangle with legs x and y.

By Pythagoras theorem:

$$z^2 = x^2 + y^2$$

$$\Rightarrow z^2 = 16^2 + 12^2$$

$$\Rightarrow z^2 = 256 + 144$$

$$\Rightarrow z^2 = 400$$

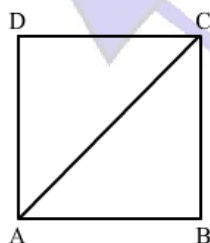
$$\Rightarrow z^2 = 20^2$$

$$\Rightarrow z = 20$$

Hence, the length of the diagonal is 20 cm.

Q. 16

Answer :



$$AB = 40 \text{ cm}$$

$$\text{Diagonal, } AC = 41 \text{ cm}$$

Then, by Pythagoras theorem in right $\triangle ABC$:

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow BC^2 = 41^2 - 40^2$$

$$\Rightarrow BC^2 = 1681 - 1600$$

$$\Rightarrow BC^2 = 81$$

$$\Rightarrow BC^2 = 9^2$$

$$\Rightarrow BC = 9 \text{ cm}$$

$$\therefore \text{Length} = 40 \text{ cm}$$

$$\text{Breadth} = 9 \text{ cm}$$

$$\begin{aligned}\therefore \text{Perimeter of the rectangle} &= 2(\text{length} + \text{breadth}) \\ &= 2(40+9) \\ &= 98 \text{ cm}\end{aligned}$$

Q. 17

Answer :

We know that the diagonals of a rhombus bisect each other at right angles.

Therefore, in right triangle AOB, we have:

$$AO = 8 \text{ cm}$$

$$BO = 15 \text{ cm}$$

By Pythagoras theorem in $\triangle AOB$:

$$AB^2 = AO^2 + BO^2$$

$$\Rightarrow AB^2 = 8^2 + 15^2$$

$$\Rightarrow AB^2 = 64 + 225$$

$$\Rightarrow AB^2 = 289$$

$$\Rightarrow AB^2 = 17^2$$

$$\Rightarrow AB = 17 \text{ cm}$$

Now, as we know that all sides of a rhombus are equal.

$$\begin{aligned}\therefore \text{Perimeter of the rhombus} &= 4(\text{side}) \\ &= 4(17) \\ &= 68 \text{ cm}\end{aligned}$$

Q. 18

Answer :

(i) In a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

(ii) If the square of one side of a triangle is equal to the sum of the squares of the other two sides then the triangle is right angled.

(iii) Of all the line segments that can be drawn to a given line from a given point outside it, the perpendicular is the shortest.

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